## Exercise 51

For the following exercises, which of the tables could represent a linear function? For each that could be linear, find a linear equation that models the data.

| $x$ | 0 | 2 | 4 | 6 |
| :---: | :---: | :---: | :---: | :---: |
| $g(x)$ | 6 | -19 | -44 | -69 |

## Solution

This table represents a linear function because as $x$ increases by $2, g(x)$ increases by -25 . Two points on this line are

$$
(0,6) \text { and }(2,-19) .
$$

The general equation for a line is

$$
y=m x+b .
$$

The first point says that when $x=0, y=6$.

$$
6=m(0)+b
$$

The second point says that when $x=2, y=-19$.

$$
-19=m(2)+b
$$

This is a system of two equations with two unknowns that can be solved.

$$
\left\{\begin{aligned}
b & =6 \\
2 m+b & =-19
\end{aligned}\right.
$$

Substitute the value of $b$ into the second equation.

$$
2 m+(6)=-19
$$

Solve for $m$.

$$
\begin{aligned}
2 m & =-25 \\
m & =-\frac{25}{2}
\end{aligned}
$$

Now that $m$ and $b$ have been solved for, the line is known.

$$
y=-\frac{25}{2} x+6
$$

